

**KARACHI UNIVERSITY BUSINESS SCHOOL  
UNIVERSITY OF KARACHI**

<b><u>BS (BBA) – VI</u></b>	
<b>Course Title</b>	<b>: STATISTICS</b>
<b>Course Number</b>	<b>: BA(BS) – 532</b>
<b>Credit Hours</b>	<b>: 03</b>

**Course Contents**

**1. Statistical Concepts and Market Returns**

- 1.1. distinguish between descriptive statistics and inferential statistics, between a population and a sample, and among the types of measurement scales;
- 1.2. define a parameter, a sample statistic, and a frequency distribution;
- 1.3. calculate and interpret relative frequencies and cumulative relative frequencies, given a frequency distribution;
- 1.4. describe the properties of a data set presented as a histogram or a frequency polygon;
- 1.5. calculate and interpret measures of central tendency, including the population mean, sample mean, arithmetic mean, weighted average or mean, geometric mean, harmonic mean, median, and mode;
- 1.6. calculate and interpret quartiles, quintiles, deciles, and percentiles;
- 1.7. calculate and interpret
- 1.8. a range and a mean absolute deviation and
- 1.9. the variance and standard deviation of a population and of a sample;
- 1.10. calculate and interpret the proportion of observations falling within a specified number of standard deviations of the mean using Chebyshev's inequality;
- 1.11. calculate and interpret the coefficient of variation and the Sharpe ratio;
- 1.12. explain skewness and the meaning of a positively or negatively skewed return distribution;
- 1.13. describe the relative locations of the mean, median, and mode for a uni-modal, nonsymmetrical distribution;
- 1.14. explain measures of sample skewness and kurtosis;
- 1.15. compare the use of arithmetic and geometric means when analyzing investment returns.

**Contents**

Fundamental Concepts  
Summarizing data using frequency distribution  
The graphical representation of the data  
Measure of central tendency  
Other measures of location: Quantiles

Measurement of dispersion  
Symmetry and Skewness in return distribution

## 2. Probability Concepts

- 2.1. define a random variable, an outcome, an event, mutually exclusive events, and exhaustive events;
- 2.2. state the two defining properties of probability and distinguish among empirical, subjective, and a priori probabilities;
- 2.3. state the probability of an event in terms of odds for and against the event;
- 2.4. distinguish between unconditional and conditional probabilities;
- 2.5. explain the multiplication, addition, and total probability rules;
- 2.6. calculate and interpret
  - 2.6.1. the joint probability of two events,
  - 2.6.2. the probability that at least one of two events will occur, given the probability of each and the joint probability of the two events, and
  - 2.6.3. a joint probability of any number of independent events;
- 2.7. distinguish between dependent and independent events;
- 2.8. calculate and interpret an unconditional probability using the total probability rule;
- 2.9. explain the use of conditional expectation in investment applications;
- 2.10. explain the use of a tree diagram to represent an investment problem;
- 2.11. calculate and interpret covariance and correlation;
- 2.12. calculate and interpret the expected value, variance, and standard deviation of a random variable and of returns on a portfolio;
- 2.13. calculate and interpret covariance given a joint probability function;
- 2.14. calculate and interpret an updated probability using Bayes' formula;
- 2.15. identify the most appropriate method to solve a particular counting problem, and solve counting problems using factorial, combination, and permutation concepts.

### Contents

Probability, Expected value and variance  
Portfolio expected return and variance of return  
Bayes' Formula, Principles of counting

## 3. Common Probability Distributions

- 3.1. define a probability distribution and distinguish between discrete and continuous random variables and their probability functions;
- 3.2. describe the set of possible outcomes of a specified discrete random variable;
- 3.3. interpret a cumulative distribution function;
- 3.4. calculate and interpret probabilities for a random variable, given its cumulative distribution function;
- 3.5. define a discrete uniform random variable, a Bernoulli random variable, and a binomial random variable;
- 3.6. calculate and interpret probabilities given the discrete uniform and the binomial distribution functions;
- 3.7. construct a binomial tree to describe stock price movement;
- 3.8. calculate and interpret tracking error;
- 3.9. define the continuous uniform distribution and calculate and interpret probabilities, given a continuous uniform distribution;

- 3.10. explain the key properties of the normal distribution;
- 3.11. distinguish between a uni-variate and a multivariate distribution, and explain the role of correlation in the multivariate normal distribution;
- 3.12. determine the probability that a normally distributed random variable lies inside a given interval;
- 3.13. define the standard normal distribution, explain how to standardize a random variable, and calculate and interpret probabilities using the standard normal distribution;
- 3.14. define shortfall risk, calculate the safety–first ratio, and select an optimal portfolio using Roy’s safety–first criterion;
- 3.15. explain the relationship between normal and lognormal distributions and why the lognormal distribution is used to model asset prices;
- 3.16. distinguish between discretely and continuously compounded rates of return, and calculate and interpret a continuously compounded rate of return, given a specified holding period return;
- 3.17. Explain Monte Carlo simulation and describe its applications and limitations;
- 3.18. Compare Monte Carlo simulation and historical simulation.

### **Contents**

Discrete Random variable  
Continuous Random Variable  
Monte Carlo Simulation

## **4. Sampling and Estimation**

- 4.1. Define simple random sampling and a sampling distribution;
- 4.2. Explain sampling error;
- 4.3. Distinguish between simple random and stratified random sampling;
- 4.4. Distinguish between time–series and cross–sectional data;
- 4.5. Explain the central limit theorem and its importance;
- 4.6. Calculate and interpret the standard error of the sample mean;
- 4.7. Identify and describe desirable properties of an estimator;
- 4.8. Distinguish between a point estimate and a confidence interval estimate of a Population parameter;
- 4.9. Describe properties of Student’s  $t$ –distribution and calculate and interpret its Degrees of freedom;
- 4.10. Calculate and interpret a confidence interval for a population mean, given a Normal distribution with
  - 4.10.1. A known population variance,
  - 4.10.2. An unknown population variance, or
  - 4.10.3. An unknown variance and a large sample size;
- 4.11. Describe the issues regarding selection of the appropriate sample size, data mining bias, sample selection bias, survivorship bias, look–ahead bias, and time period bias.

**Contents**

Sampling  
Distribution of Sample mean  
Point and interval estimate of the population mean  
More on sampling

**5. Hypothesis Testing**

- 5.1. Define a hypothesis, describe the steps of hypothesis testing, and describe and interpret the choice of the null and alternative hypotheses;
- 5.2. Distinguish between one-tailed and two-tailed tests of hypotheses;
- 5.3. Explain a test statistic, Type I and Type II errors, a significance level, and how Significance levels are used in hypothesis testing;
- 5.4. Explain a decision rule, the power of a test, and the relation between confidence Intervals and hypothesis tests;
- 5.5. Distinguish between a statistical result and an economically meaningful result;
- 5.6. Explain and interpret the  $p$ -value as it relates to hypothesis testing;
- 5.7. Identify the appropriate test statistic and interpret the results for a hypothesis test concerning the population mean of both large and small samples when the population is normally or approximately distributed and the variance is
  - 5.7.1. Known
  - 5.7.2. Unknown;
- 5.8. Identify the appropriate test statistic and interpret the results for a hypothesis test concerning the equality of the population means of two at least approximately normally distributed populations, based on independent random samples with
  - 5.8.1. Equal or
  - 5.8.2. Unequal assumed variances;
- 5.9. Identify the appropriate test statistic and interpret the results for a hypothesis test concerning the mean difference of two normally distributed populations;
- 5.10. Identify the appropriate test statistic and interpret the results for a hypothesis test concerning
  - 5.10.1. The variance of a normally distributed population, and
  - 5.10.2. The equality of the variances of two normally distributed populations based on two independent random samples;
- 5.11. Distinguish between parametric and nonparametric tests and describe situations in which the use of nonparametric tests may be appropriate.

**Contents**

Hypothesis testing;  
Hypothesis tests concerning the mean  
Hypothesis tests concerning the variance  
Non Parametric Inference

**6. Correlation and Regression**

- 6.1. Calculate and interpret a sample covariance and a sample correlation coefficient, and interpret a scatter plot;
- 6.2. Describe limitations to correlation analysis;

- 6.3. Formulate a test of the hypothesis that the population correlation coefficient equals zero, and determine whether the hypothesis is rejected at a given level of significance;
- 6.4. Distinguish between the dependent and independent variables in a linear regression;
- 6.5. Describe the assumptions underlying linear regression, and interpret regression coefficients;
- 6.6. Calculate and interpret the standard error of estimate, the coefficient of determination, and a confidence interval for a regression coefficient;
- 6.7. Formulate a null and alternative hypothesis about a population value of a regression coefficient, and determine the appropriate test statistic and whether the null hypothesis is rejected at a given level of significance;
- 6.8. Calculate the predicted value for the dependent variable, given an estimated regression model and a value for the independent variable;
- 6.9. Calculate and interpret a confidence interval for the predicted value of the dependent variable;
- 6.10. Describe the use of analysis of variance (ANOVA) in regression analysis, interpret ANOVA results, and calculate and interpret the  $F$ -statistic;
- 6.11. Describe limitations of regression analysis.

### **Contents**

Introduction  
Correlation Analysis  
Linear Regression

### **Recommended Books:**

1. Bluman, A. G. (2003). *Elementary Statistics: A Brief Version*. McGraw–Hill.
2. Freund, J. E. (2003). *Mathematical Statistics with Applications*. Prentice Hall.
3. Spiegel, M. R. (2000). *Schaum's Outline of Probability and Statistics*. McGraw–Hill.
4. Weiss, N. A. (2004). *Introductory Statistics*, 7<sup>th</sup> Edition, Addison–Wesley.